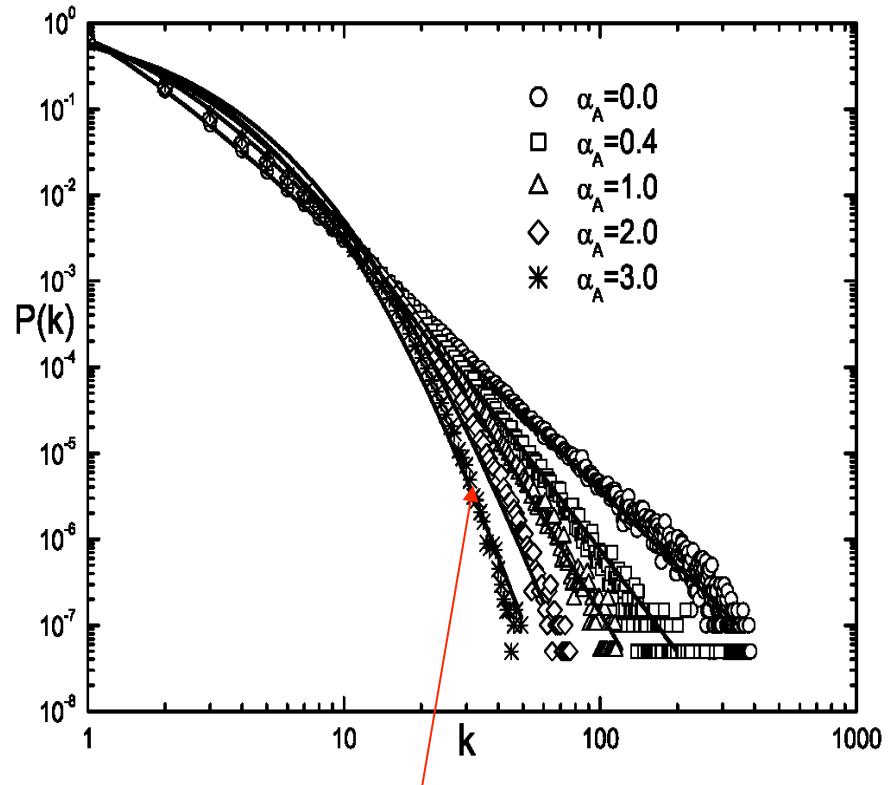
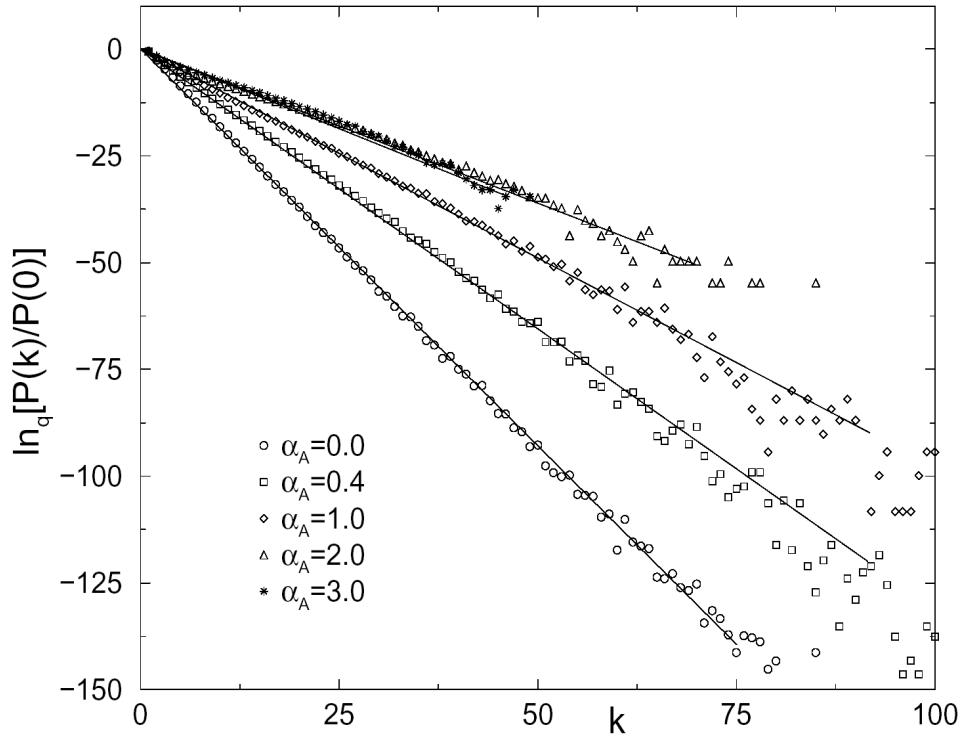


2000 realizations of  $N = 10000$  networks

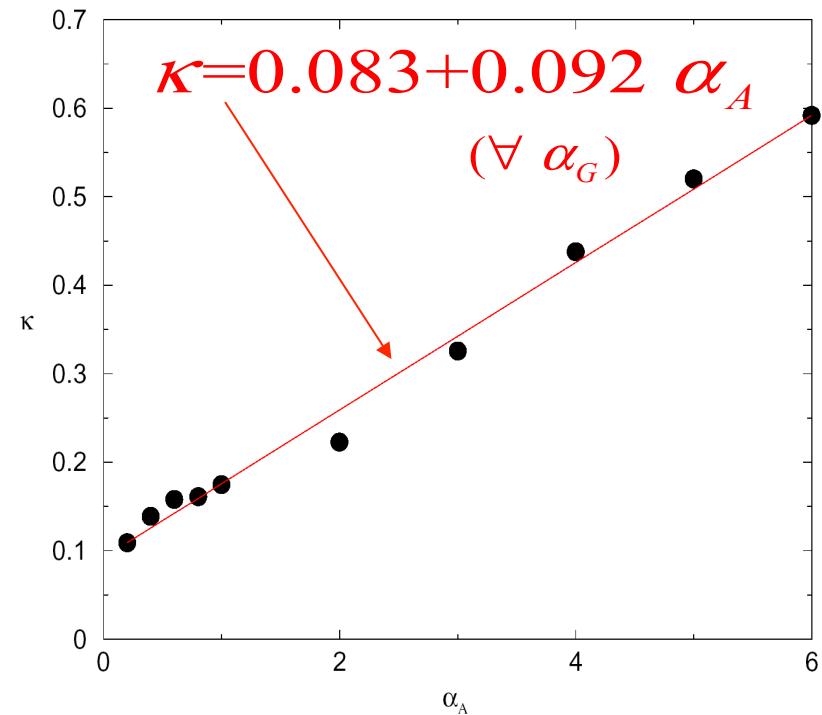
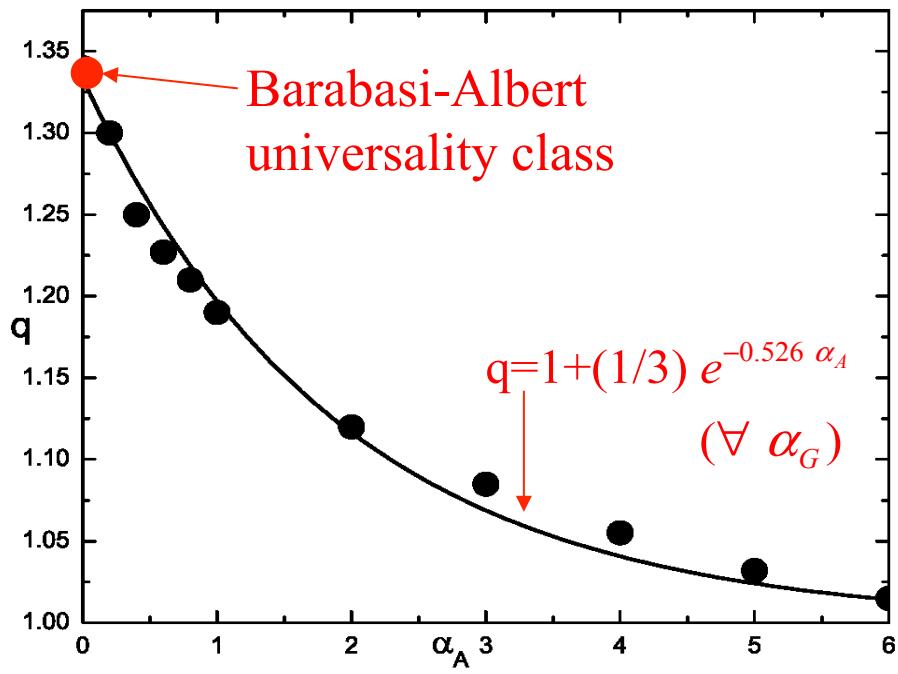


$$P(k)/P(0) = e_q^{-k/\kappa}$$

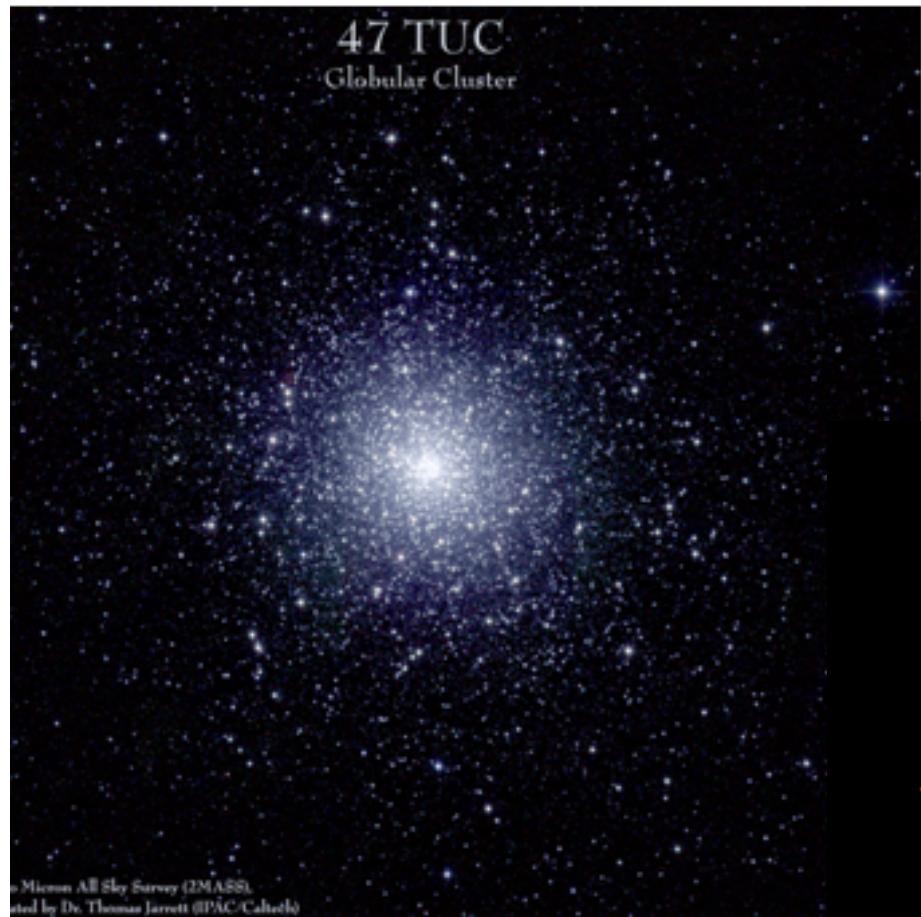
$$\equiv 1/[1 + (q-1)k/\kappa]^{1/(q-1)}$$



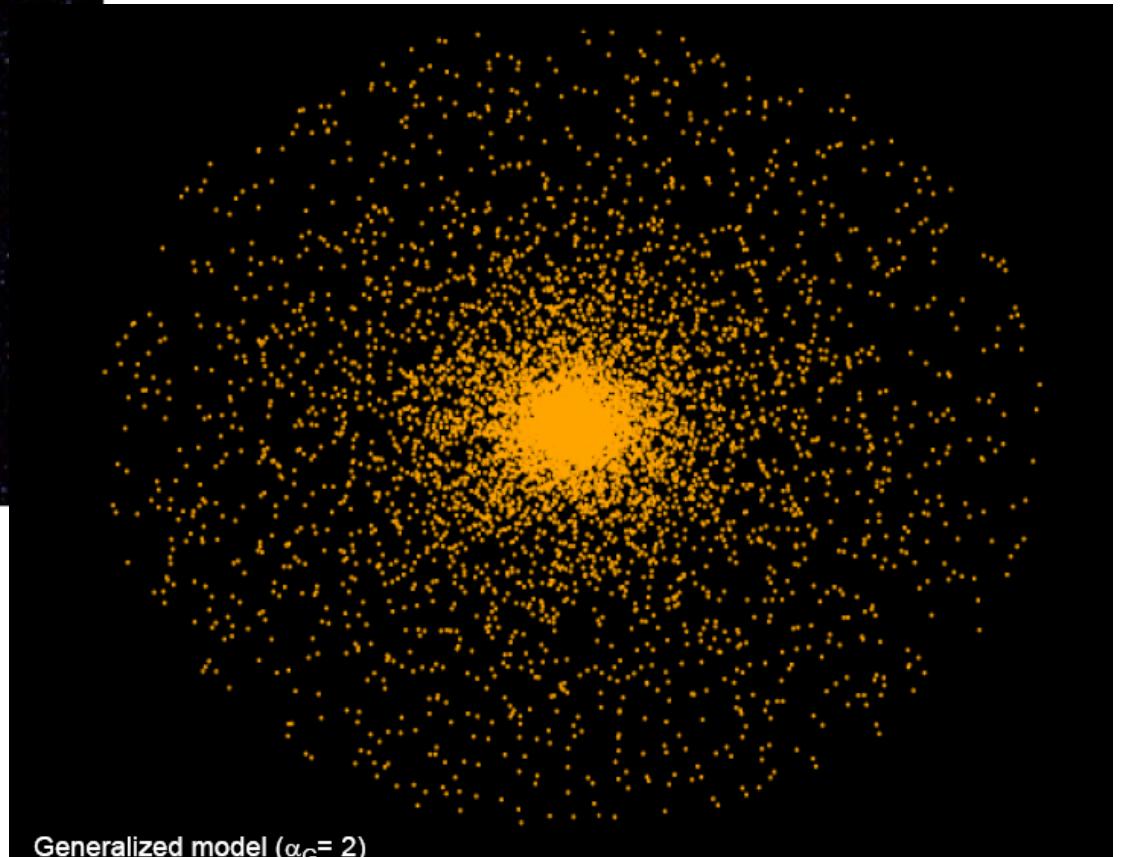
D.J.B. Soares, C. T., A.M. Mariz and L.R. Silva  
Europhys Lett 70, 70 (2005)



## SCALE-FREE NETWORKS:



D.J.B. Soares, C. T., A.M. Mariz  
and L.R. da Silva  
Europhys. Lett. 70, 70 (2005)



## GAS-LIKE (NODE COLLAPSING) NETWORK:

S. Thurner and C. T., Europhys Lett **72**, 197 (2005)

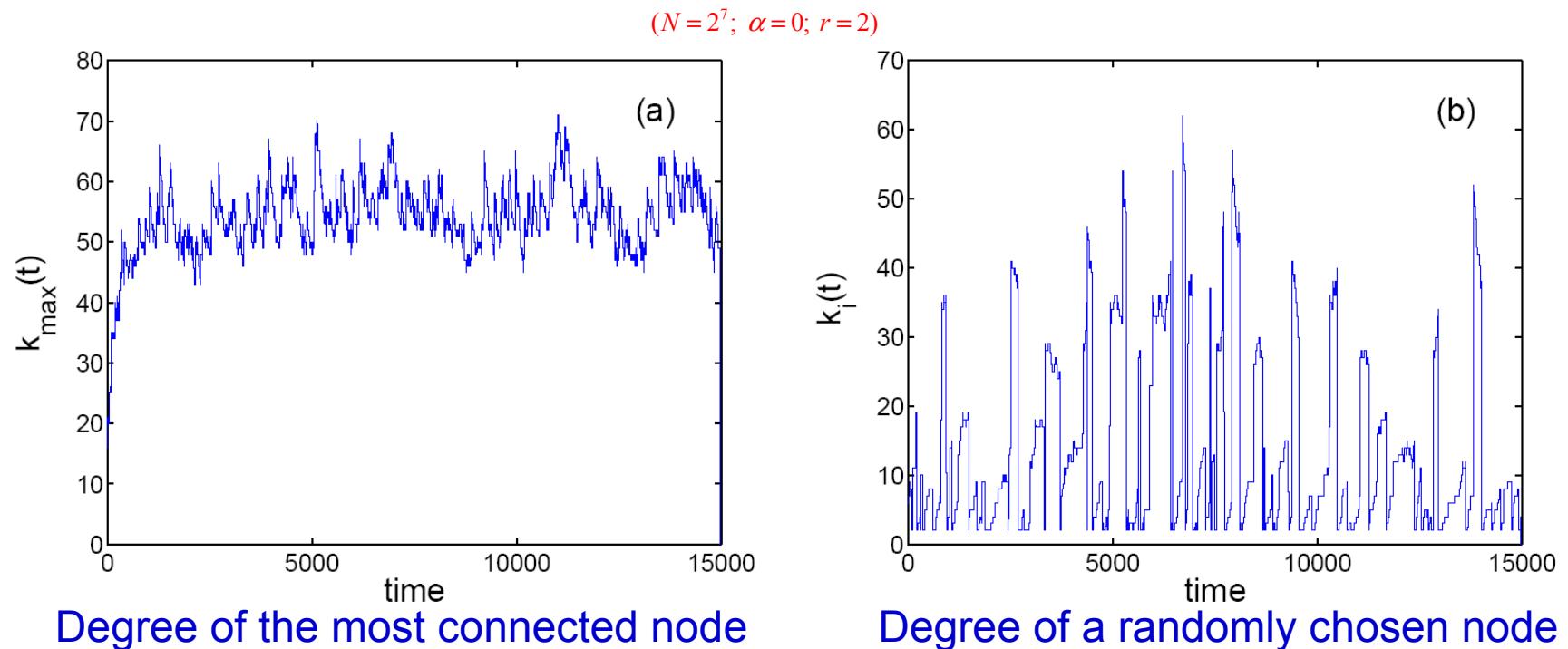
Number  $N$  of nodes fixed (*chemostat*);  $i=1, 2, \dots, N$

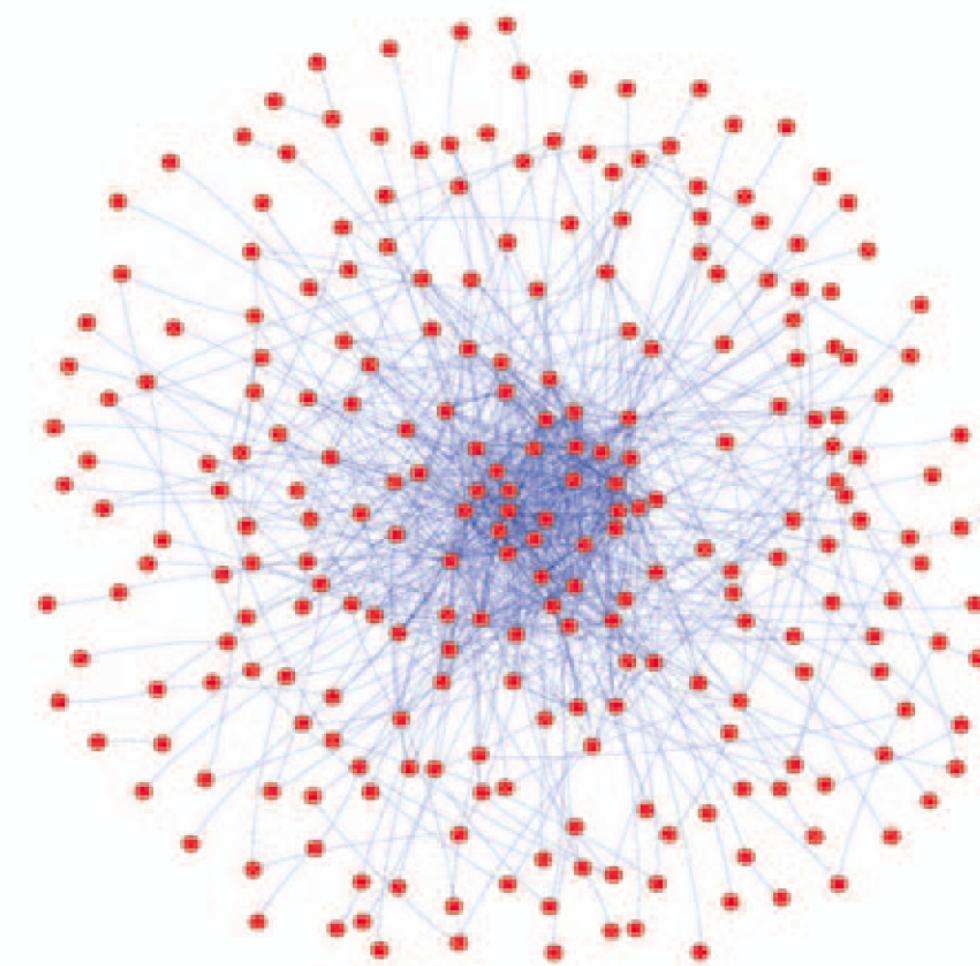
$$\text{Merging probability } p_{ij} \propto \frac{1}{d_{ij}^\alpha} \quad (\alpha \geq 0)$$

$d_{ij}$   $\equiv$  shortest path (chemical distance) connecting nodes  $i$  and  $j$  on the network

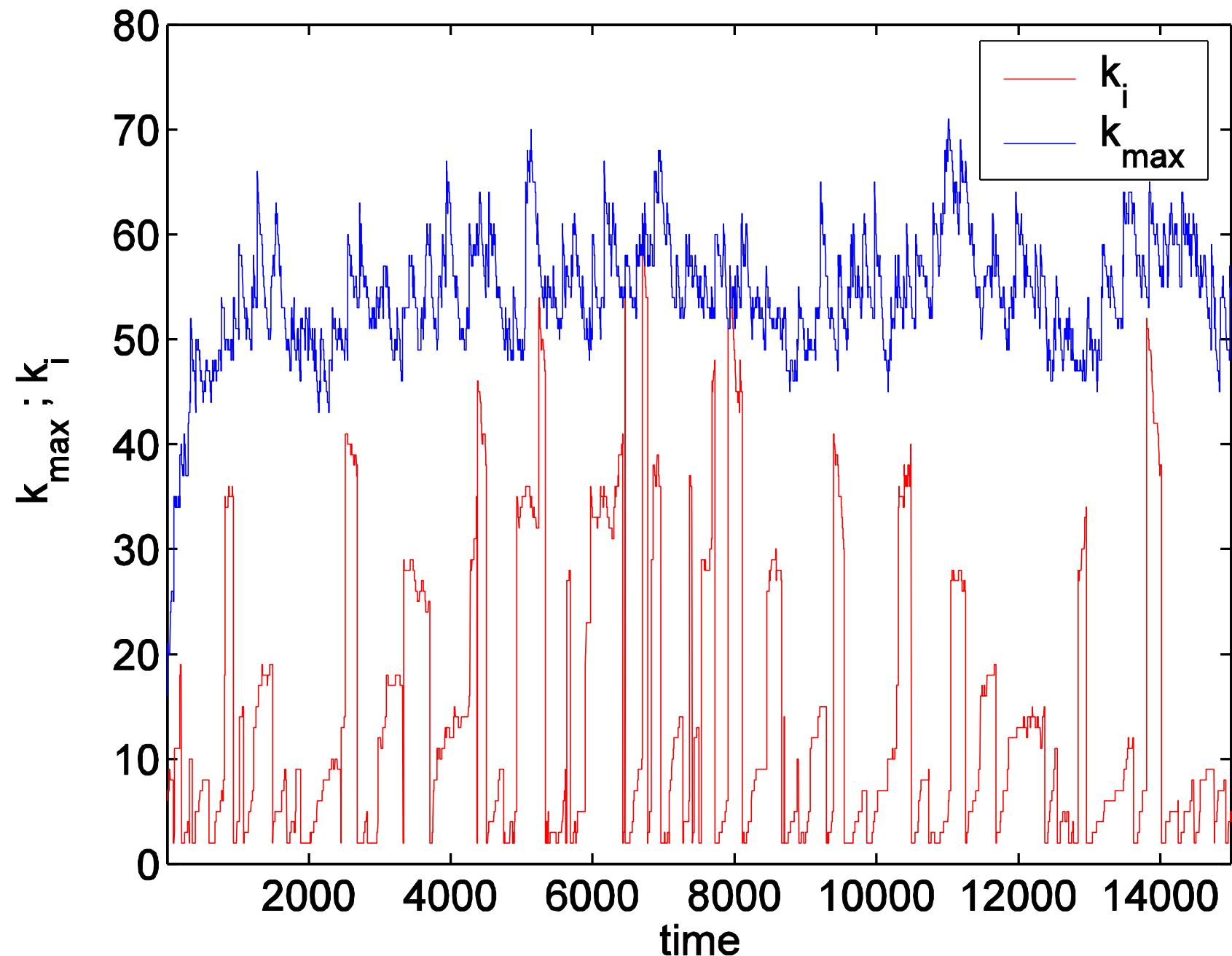
$\alpha = 0$  and  $\alpha \rightarrow \infty$  recover the *random* and the *neighbor* schemes respectively

(Kim, Trusina, Minnhagen and Sneppen, *Eur. Phys. J. B* 43 (2005) 369)

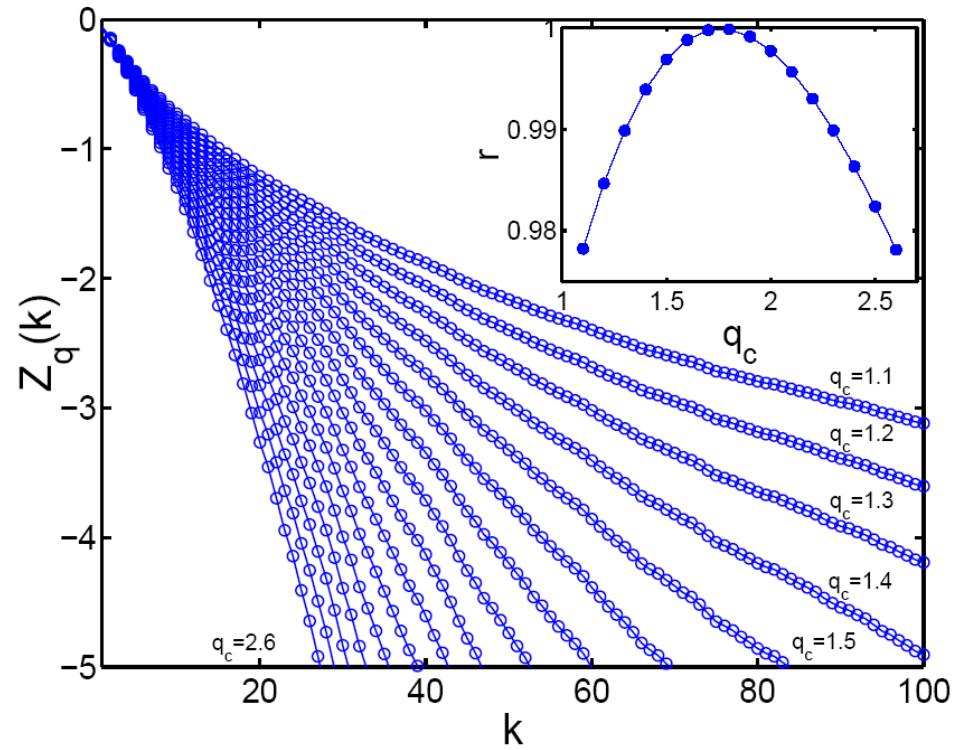
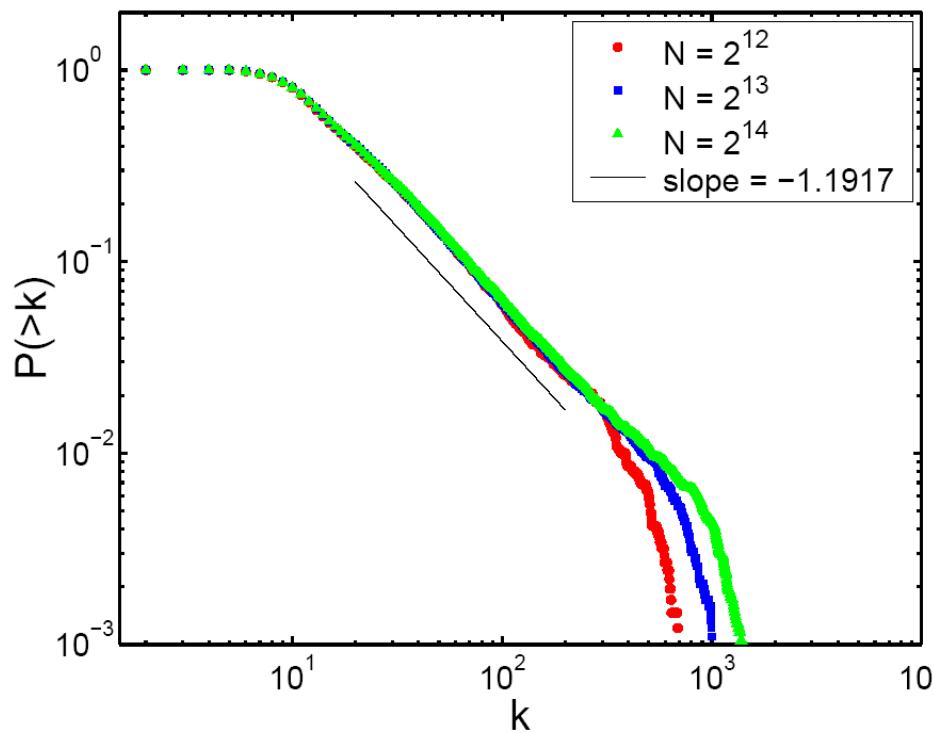




▲ **Fig. 1:** Snapshot of a non-growing dynamic network with  $q$ -exponential degree distribution for  $N = 256$  nodes and a linking rate of  $\bar{r} = 1$ , for details see [8, 9]. The shown network is small to make connection patterns visible.



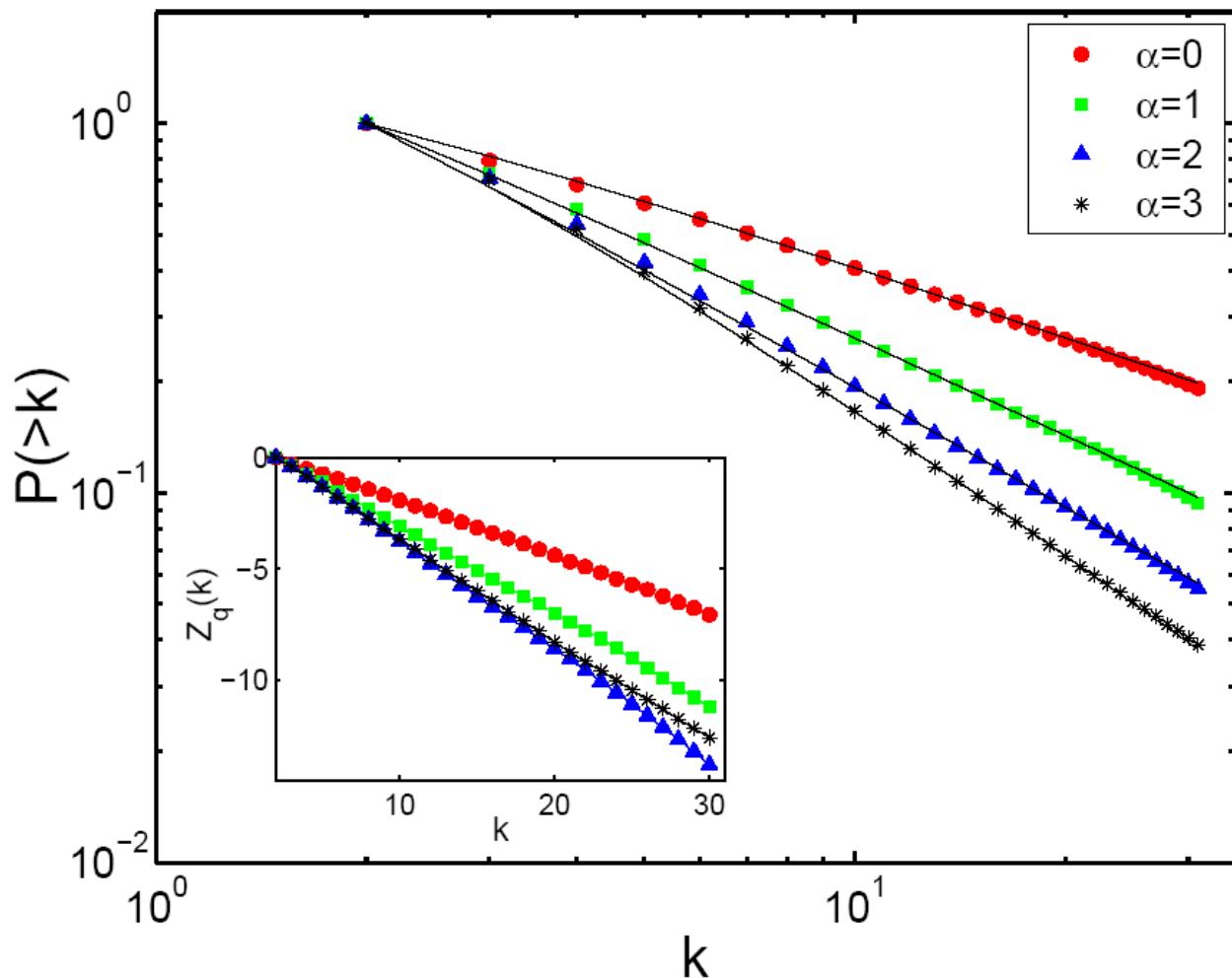
$(\alpha \rightarrow \infty ; \langle r \rangle = 8)$



$$Z_q(k) \equiv \ln_q [P(>k)] \equiv \frac{[P(>k)]^{1-q} - 1}{1-q}$$

*(optimal  $q_c = 1.84$ )*

$$(N = 2^9; r = 2)$$

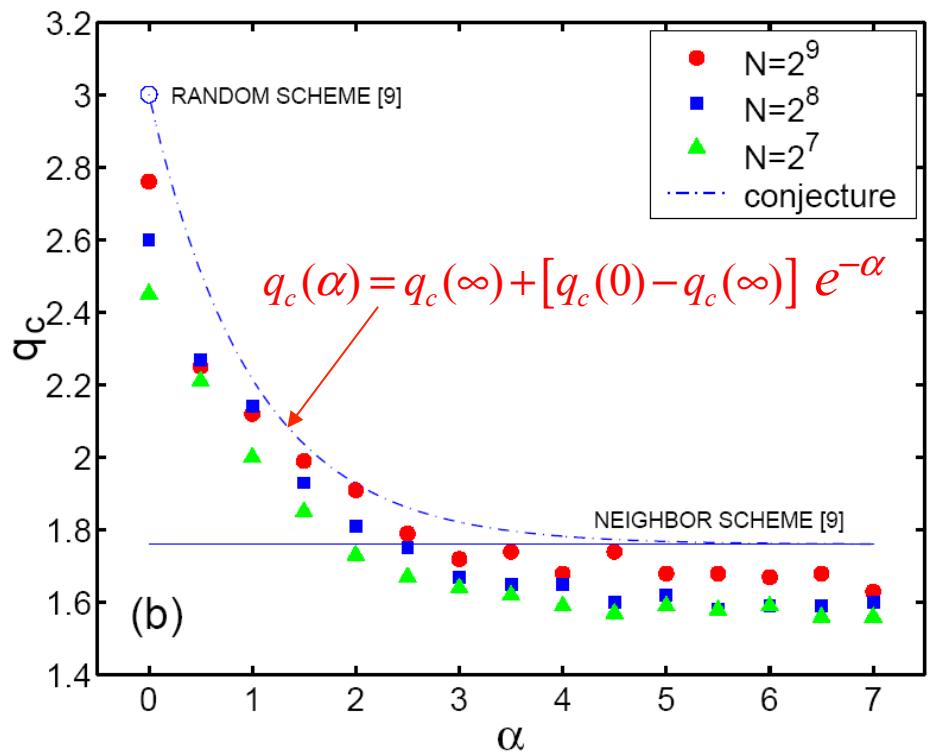
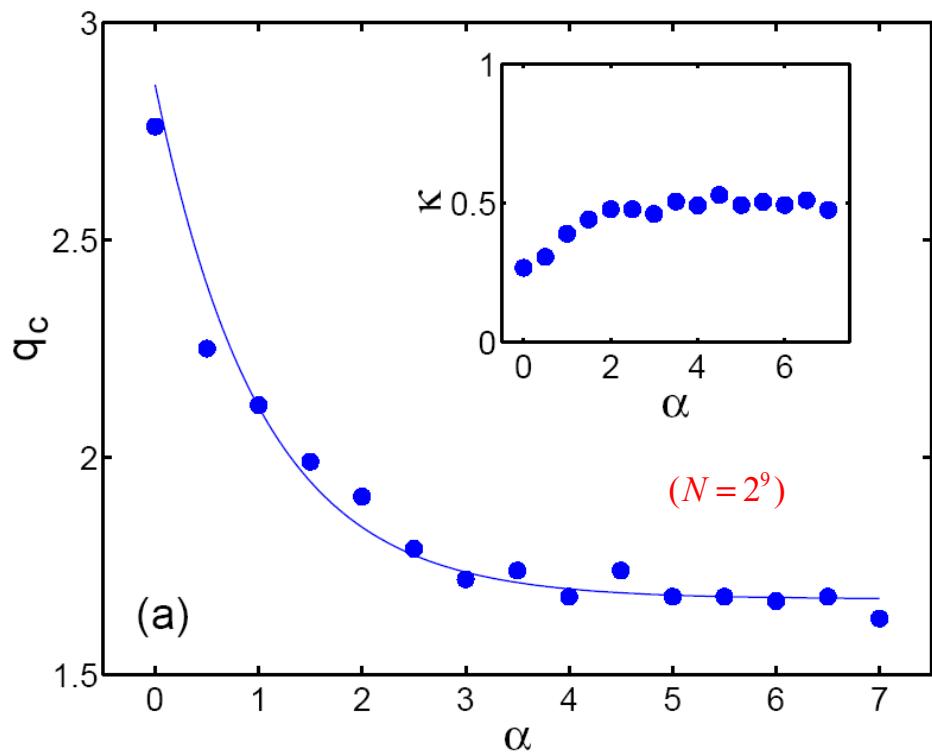


$$P(\geq k) = e_{q_c}^{-(k-2)/\kappa} \quad (k = 2, 3, 4, \dots)$$

*linear correlation*  $\in [0.999901, 0.999976]$

S. Thurner and C. T., Europhys Lett 72, 197 (2005)

$(r = 2)$



## HOW COME THE DEGREE DISTRIBUTION COINCIDES WITH THAT MAXIMIZING $S_q$ ?

*If we associate with each bond an "energy"  $\epsilon$ ,  
we may associate with each node ( $i = 1, 2, \dots, N$ ) the energy  $k_i \epsilon / 2$ .*

Therefore the degree distribution coincides with the energy distribution!

# SCIENTIFIC REPORTS



OPEN

## Role of dimensionality in complex networks

Samuráí Brito<sup>1</sup>, L. R. da Silva<sup>1,2</sup> & Constantino Tsallis<sup>2,3</sup>

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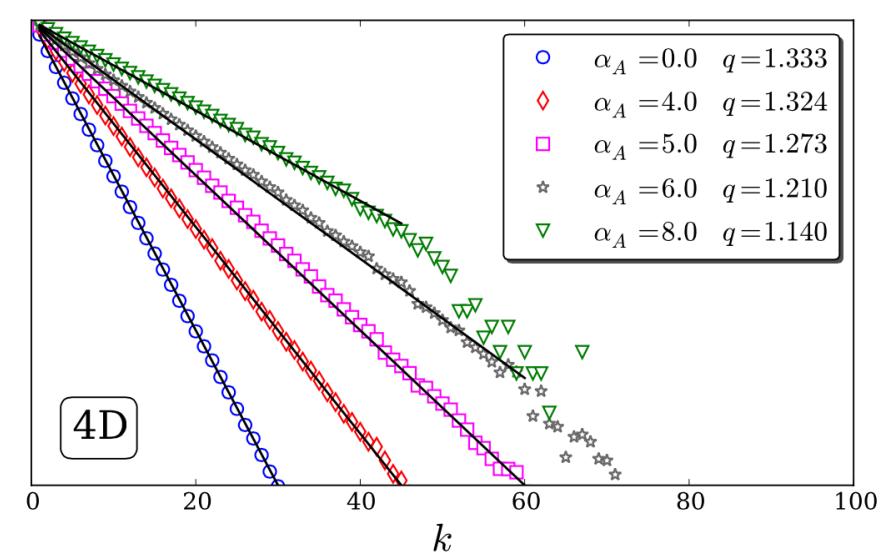
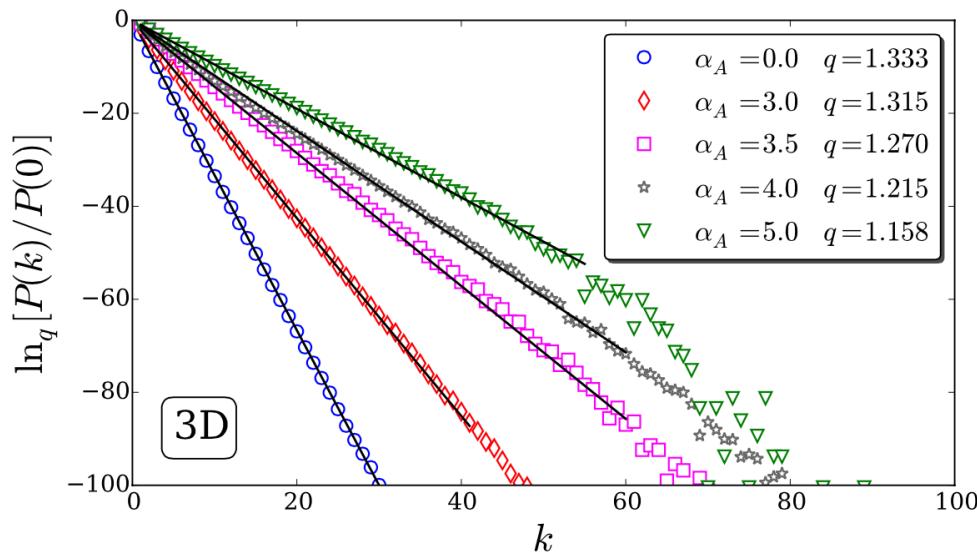
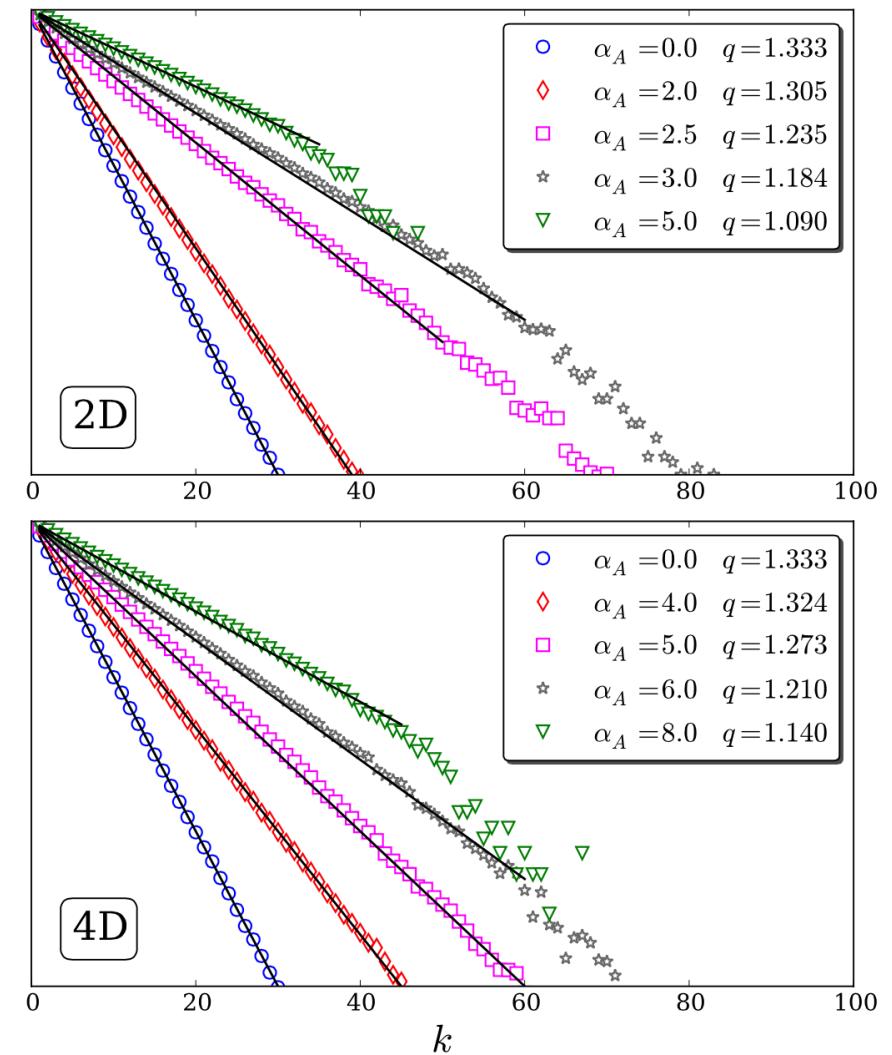
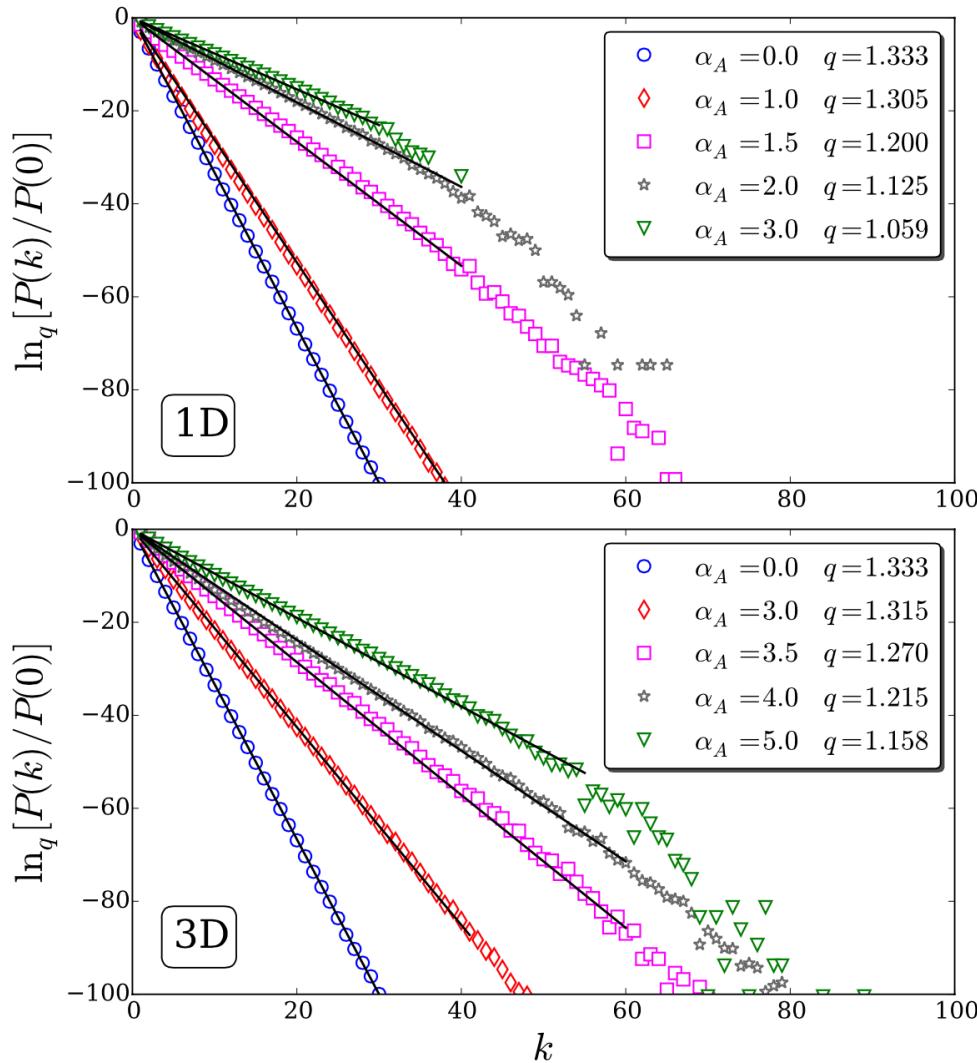
Deep connections are known to exist between scale-free networks and non-Gibbsian statistics. For example, typical degree distributions at the thermodynamical limit are of the form  $P(k) \propto e_q^{-k/\kappa}$ , where the  $q$ -exponential form  $e_q^z \equiv [1 + (1 - q)z]^{1/(1-q)}$  optimizes the nonadditive entropy  $S_q$  (which, for  $q \rightarrow 1$ , recovers the Boltzmann-Gibbs entropy). We introduce and study here  $d$ -dimensional geographically-located networks which grow with preferential attachment involving Euclidean distances through  $r_{ij}^{-\alpha}$  ( $\alpha_A \geq 0$ ). Revealing the connection with  $q$ -statistics, we numerically verify (for  $d = 1, 2, 3$  and  $4$ ) that the  $q$ -exponential degree distributions exhibit, for both  $q$  and  $k$ , universal dependences on the ratio  $\alpha_A/d$ . Moreover, the  $q = 1$  limit is rapidly achieved by increasing  $\alpha_A/d$  to infinity.

$$p(r) \begin{cases} = 0 & \text{if } 0 \leq r < 1 \\ \propto \frac{1}{r^{d+\alpha_G}} & \text{otherwise} \end{cases}$$

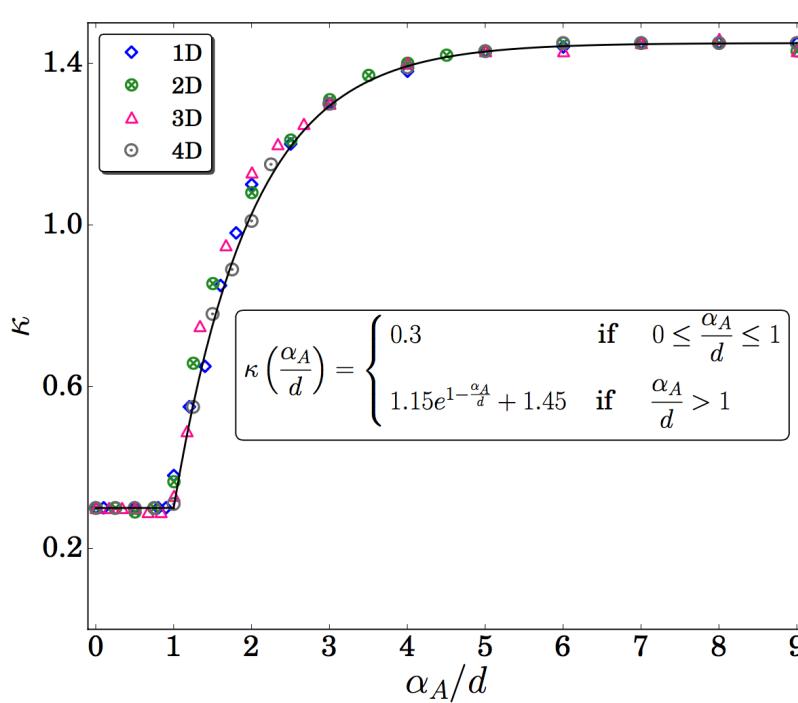
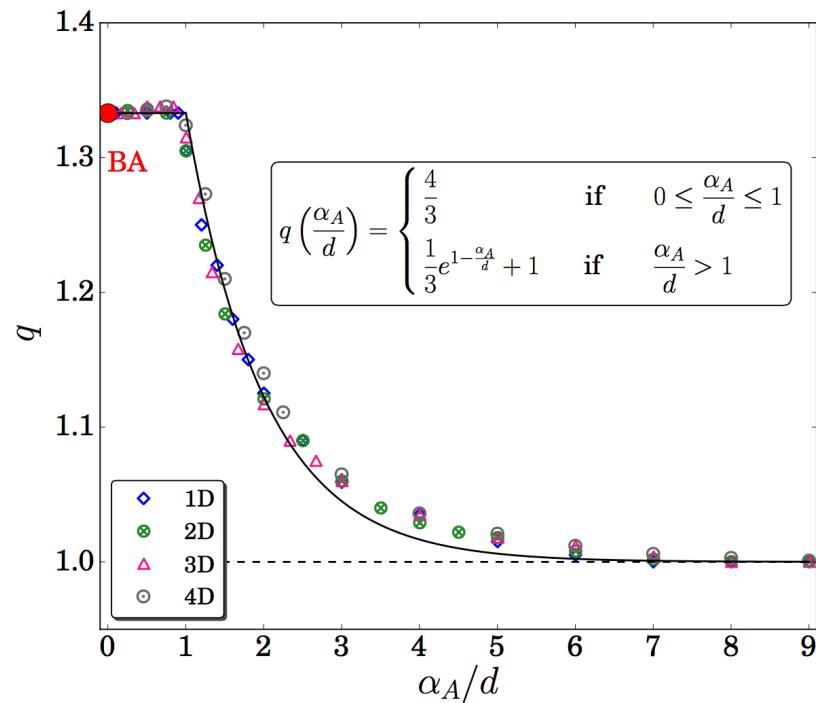
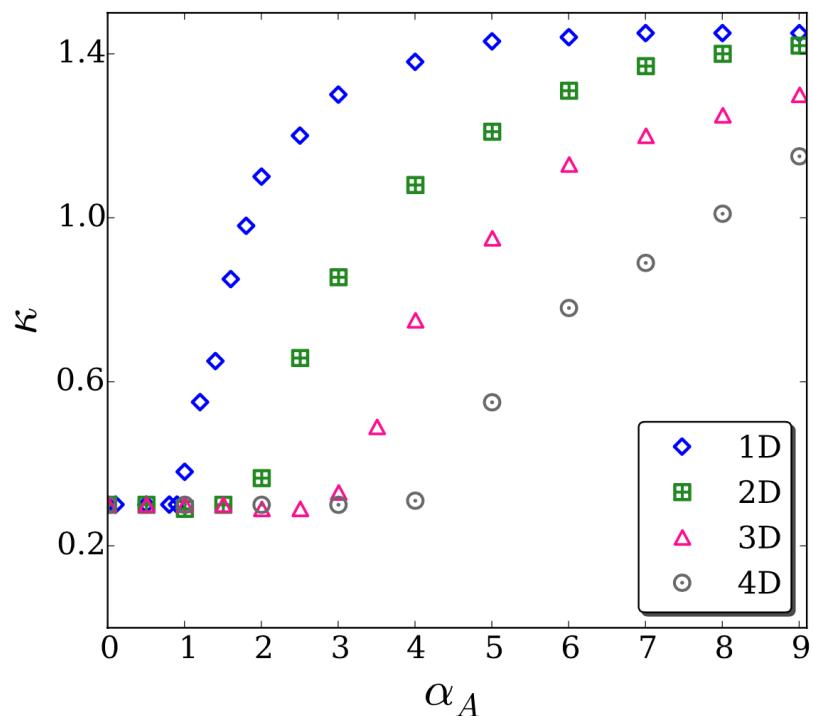
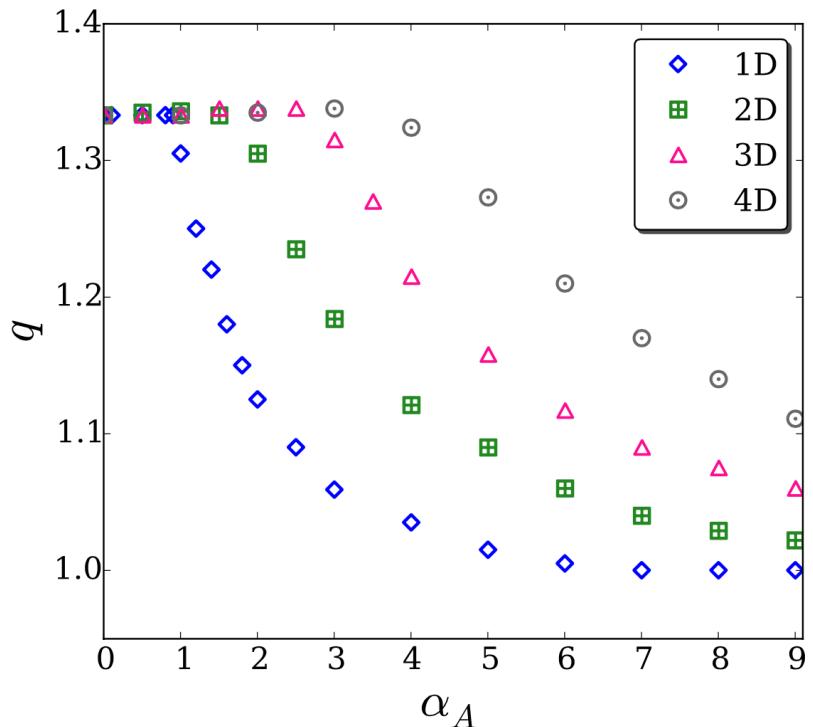
$$(\alpha_G > 0)$$

$$\Pi_{ij}(k_i) \propto \frac{k_i}{r_{ij}^{\alpha_A}}$$

$$(\alpha_A \geq 0)$$



$$P(k) = P(0) e_q^{-k/\kappa} = \frac{P(0)}{\left[1 + (q-1)k/\kappa\right]^{\frac{1}{q-1}}}$$



# LHC (Large Hadron Collider)

CMS, ALICE, ATLAS and LHCb detectors

~ 4000 scientists/engineers from ~ 200 institutions of ~ 50 countries



## Tsallis fits to $p_T$ spectra and multiple hard scattering in $pp$ collisions at the LHC

Cheuk-Yin Wong

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*National Centre for Nuclear Research, Warsaw 00-681, Poland*

(Received 12 May 2013; published 5 June 2013)

Phenomenological Tsallis fits to the CMS, ATLAS, and ALICE transverse momentum spectra of hadrons for  $pp$  collisions at LHC were recently found to extend over a large range of the transverse momentum. We investigate whether the few degrees of freedom in the Tsallis parametrization may arise from the relativistic parton-parton hard-scattering and related processes. The effects of the multiple hard-scattering and parton showering processes on the power law are discussed. We find empirically that whereas the transverse spectra of both hadrons and jets exhibit power-law behavior of  $1/p_T^n$  at high  $p_T$ , the power indices  $n$  for hadrons are systematically greater than those for jets, for which  $n \sim 4\text{--}5$ .

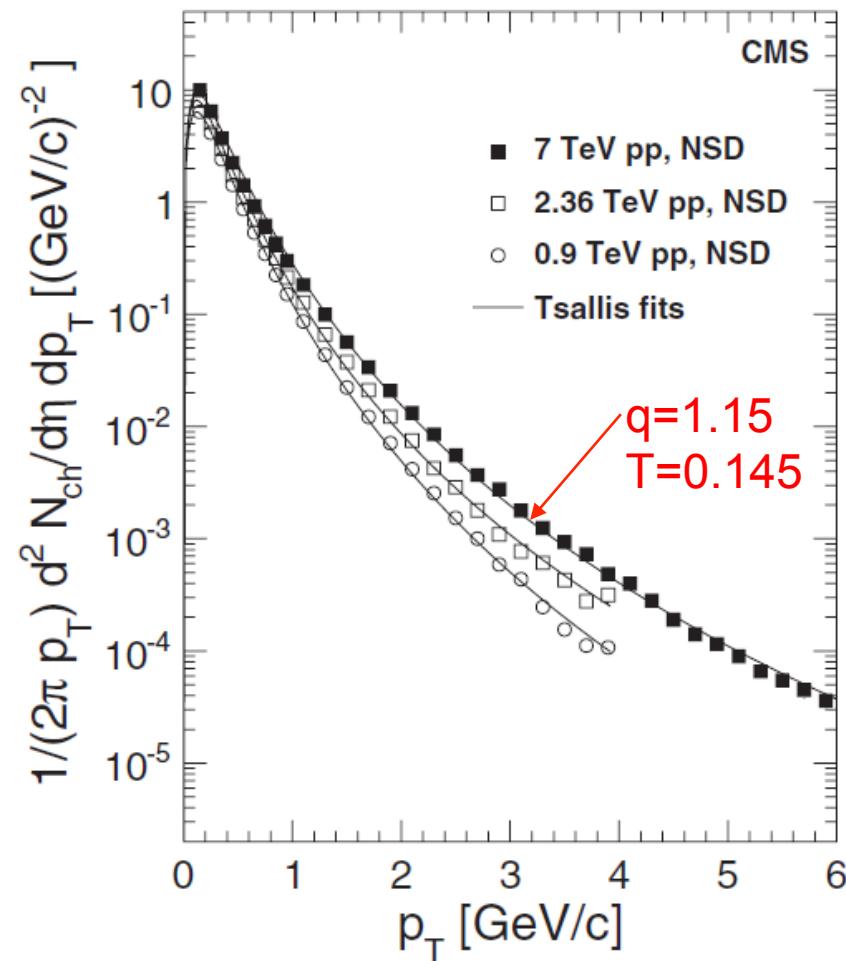
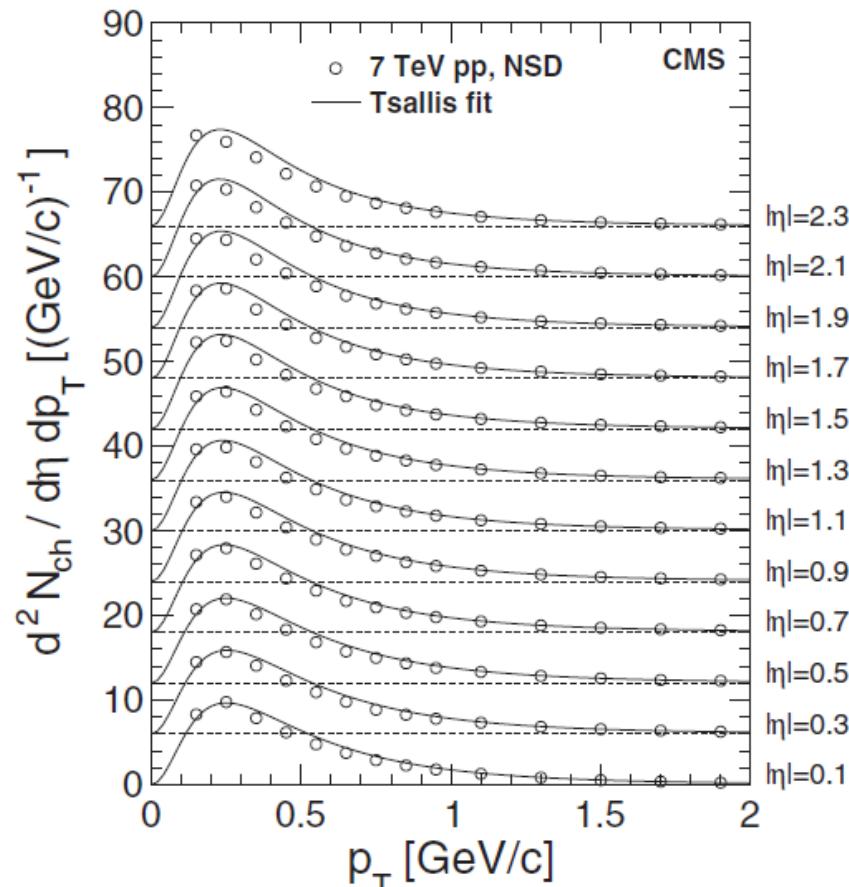


# Transverse-Momentum and Pseudorapidity Distributions of Charged Hadrons in $p p$ Collisions at $\sqrt{s} = 7$ TeV

V. Khachatryan *et al.*\*

(CMS Collaboration)

(Received 18 May 2010; published 6 July 2010)



## Tsallis fits to $p_T$ spectra and multiple hard scattering in $pp$ collisions at the LHC

Cheuk-Yin Wong

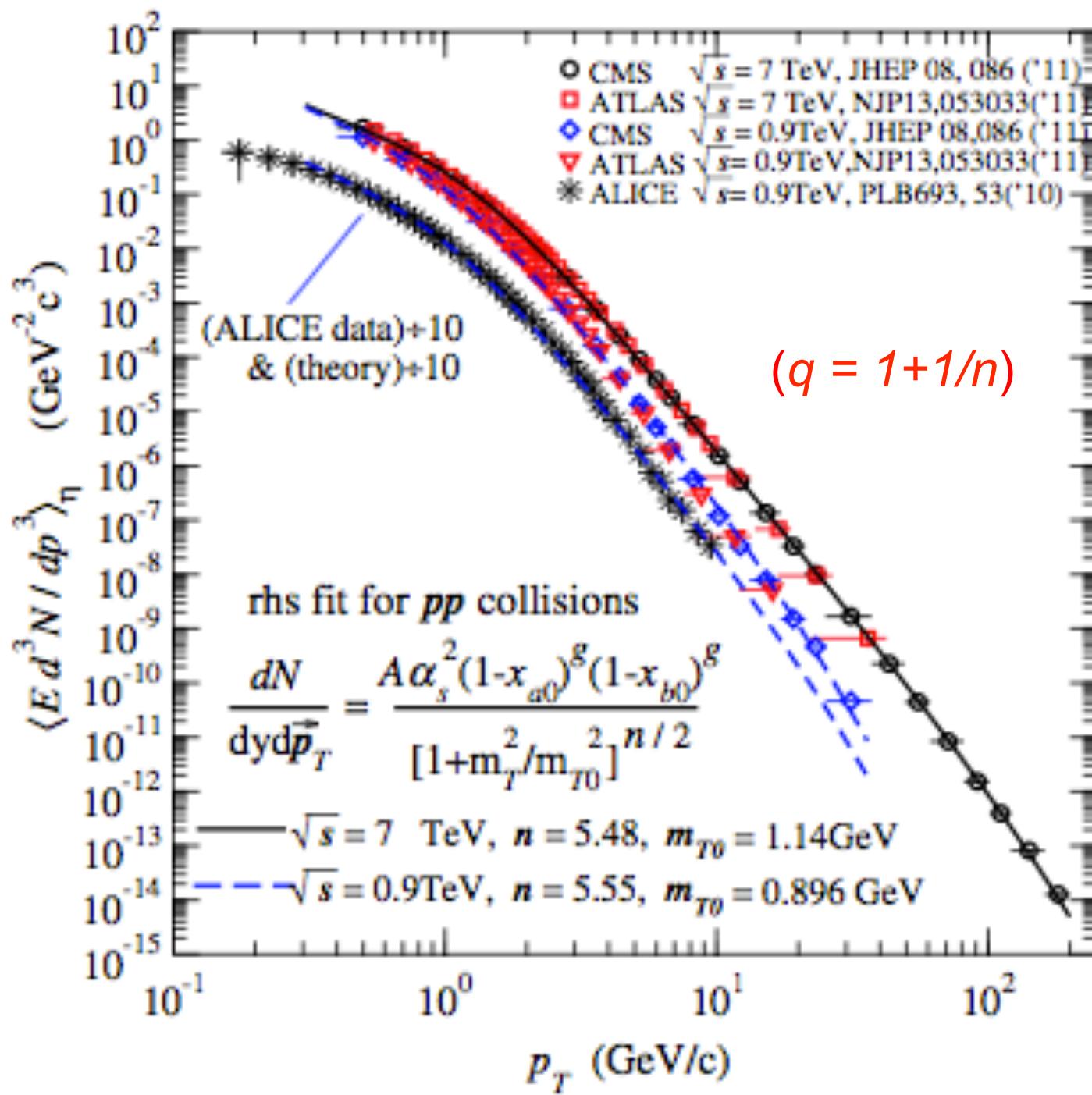
*Oak Ridge National Laboratory, Physics Division, Oak Ridge, Tennessee 37831, USA*

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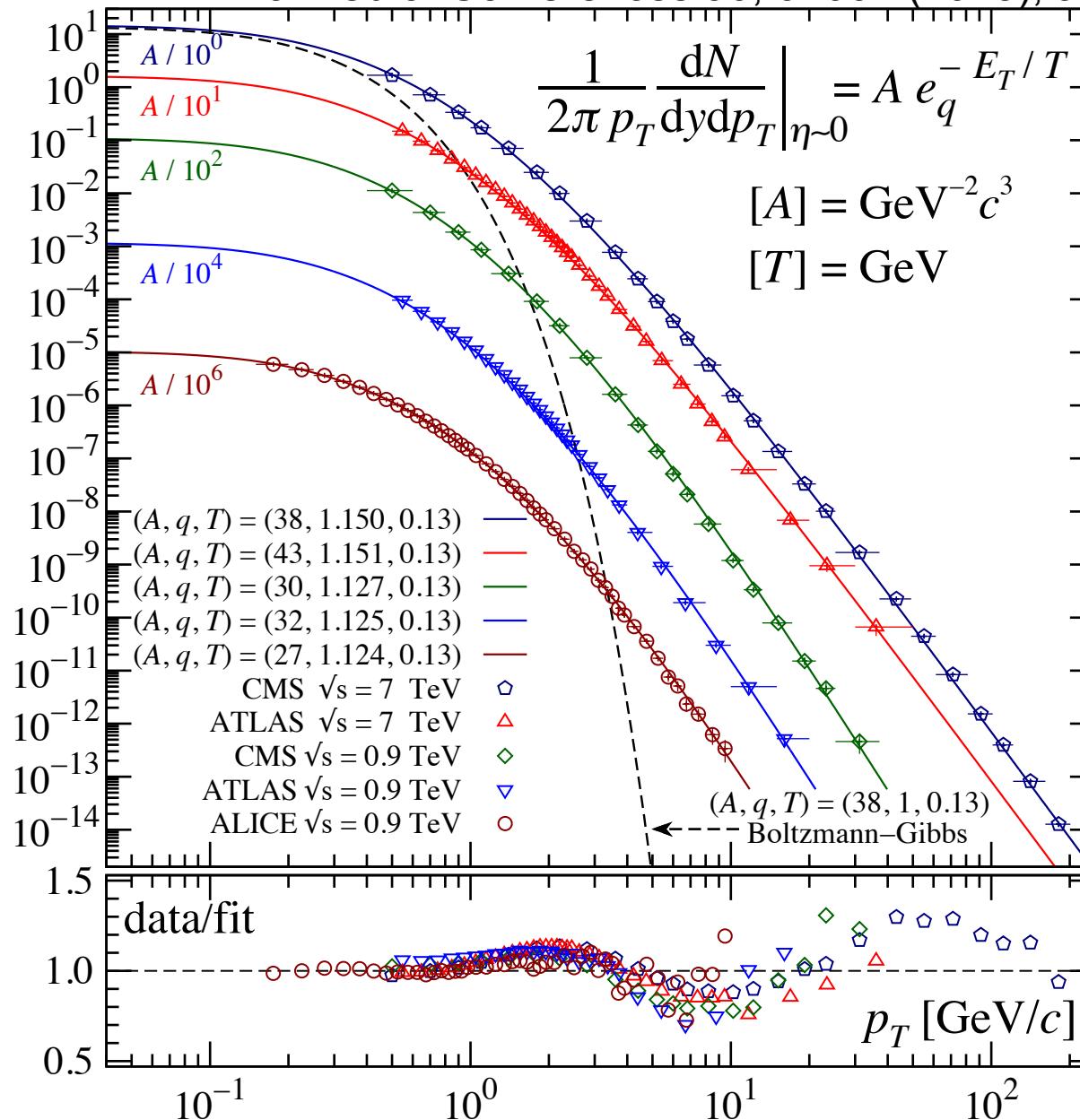
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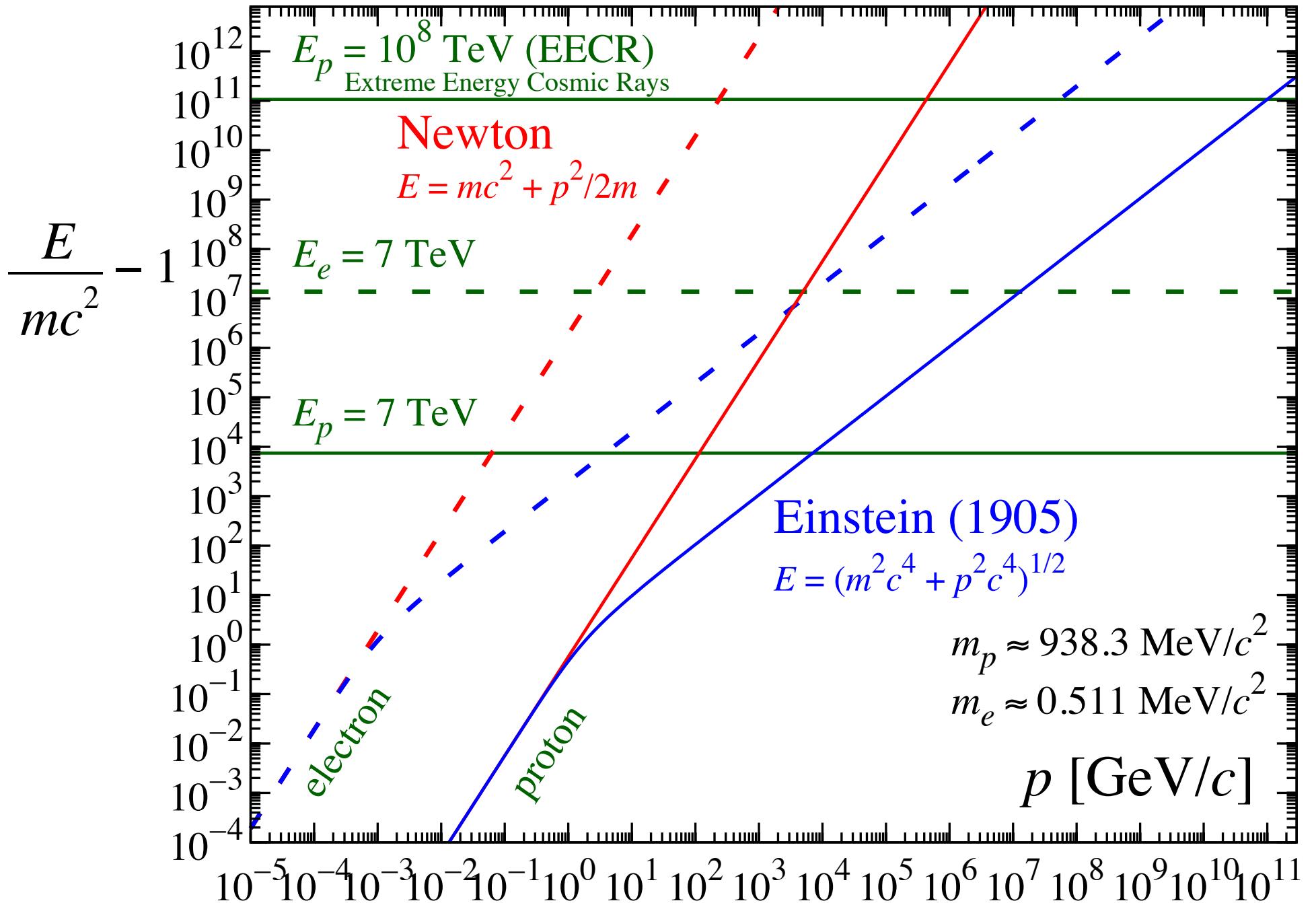
## SIMPLE APROACH: TWO-DIMENSIONAL SINGLE RELATIVISTIC FREE PARTICLE

C.Y. Wong, G. Wilk, L.J.L. Cirto and C. T.,

EPJ Web of Conferences **90**, 04002 (2015), and PRD **91**, 114027 (2015)



$$E_T = \sqrt{m^2 c^4 + p_T^2 c^2}$$



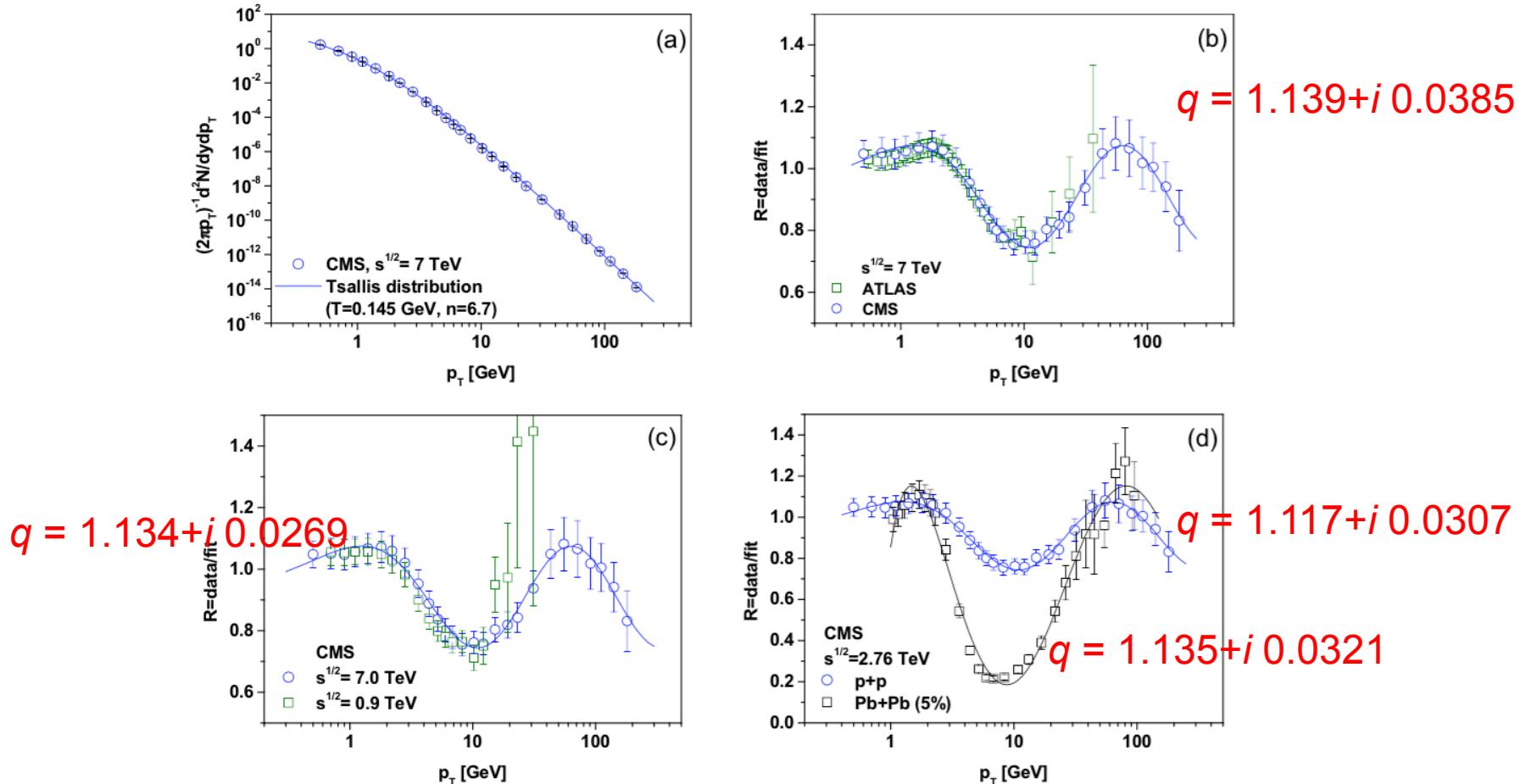
*Article*

## Tsallis Distribution Decorated with Log-Periodic Oscillation

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<sup>1</sup> Department of Fundamental Research, National Centre for Nuclear Research, Hoża 69,  
00-681 Warsaw, Poland

<sup>2</sup> Institute of Physics, Jan Kochanowski University, Świętokrzyska 15, 25-406 Kielce, Poland;  
E-Mail:zbigniew.włodarczyk@ujk.edu.pl



**Figure 1.** Examples of log-periodic oscillations. (a)  $dN/dp_T$  for the highest energy 7 TeV; the Tsallis behavior is evident. Only data from CMS experiment are shown [12]; others behave essentially in an identical manner. (b) Log-periodic oscillations showing up in different experimental data, like CMS [12] or ATLAS[15], taken at 7 TeV. (c) Results from CMS [12] for different energies. (d) Results for different systems ( $p + p$  collisions compared with  $Pb + Pb$  taken for 5% centrality [54]. Results from ALICE[55] are very similar. Fits for  $p + p$  collision at 7, 2.76 and 0.9 TeV are performed with  $q = 1.139 + i \cdot 0.0385$ ,  $1.134 + i \cdot 0.0269$  and  $1.117 + i \cdot 0.0307$ , respectively. The fit for central  $Pb + Pb$  collisions at 2.76 TeV is done with  $q = 1.135 + i \cdot 0.0321$ . See the text for more details.

**Tout le monde savait que c' était impossible.**

**Il y avait un qui ne le savait pas.**

**Alors il est allé et il l'a fait.**

**Jean Cocteau** (Marcel Pagnol, Winston Churchill, Mark Twain ...)

**Si l'action n'a quelque splendeur de liberté,  
elle n'a point de grâce ni d'honneur.**

**Montaigne**

## **Sofia e la scoperta delle fragole (Marco Bersanelli)**

A Gutenberg, tra le verdissime colline austriache, una mattina saliamo per il sentiero che attraversa il bosco scuro e profumato alle spalle del paese. Dopo mezz'ora di cammino troviamo sulla destra una sorgente presso una radura e ci fermiamo a bere. Con una grande espressione di felicità ad un tratto Sofia, la piccola di tre anni, esclama: «Mamma, mamma!! una fragola!!». Gli altri due accorrono e, constatato che la sorellina ha prontamente raccolto e inghiottito il frutto della sua scoperta, si mettono a cercare, presto seguiti dai genitori. «Un'altra!» e dopo un po': «Guarda qui, ce ne sono altre tre, quattro...». La caccia è aperta. Cercando in quel prato abbiamo presto riempito un bicchiere di fragole di bosco. Poi al ritorno, con mia sincera sorpresa, ripercorrendo lo stesso sentiero dalla sorgente in giù ne abbiamo trovate altrettante! Zero fragole all'andata, forse un centinaio al ritorno: un effetto statisticamente schiacciante. Cos'era cambiato?

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**Era  
vamo  
cambiati noi.**